Name:

# Math 115 Exam 2 

October 27, 2022

1. WRITE YOUR NAME ON THIS TEST!
2. Except where indicated, merely finding the answer to a problem is not enough to receive full credit; you must show how you arrived at that answer.
3. Unless indicated, DO NOT convert irrational numbers such as $\sqrt{3}$ or $\pi$ into decimal approximations; just leave them as they are.
4. If you have a question, raise your hand or come up and ask me.
1) Find the derivatives of the following functions:
a) $f(x)=\cos (x) \cdot\left(8 x^{5}-4 x^{2}+9 x+e^{2}\right)$
b) $g(x)=\frac{e^{x}}{17 x^{3}-12 x^{2}}$
c) $h(x)=\sin \left(\sqrt{\ln \left(x^{4}\right)}\right)$
2) Compute the equation of the tangent line to the graph of

$$
\tan \left(\pi x^{2} y^{6}\right)-\ln \left(x y^{2}\right)=1
$$

at the point $(4,1 / 2)$.
3) Determine the equation of the tangent plane to the graph of the function

$$
z=f(x, y)=e^{x^{2} y-y^{3} x}
$$

at the point $(4,2,1)$.
4) Determine the values of the following limits:
a) $\lim _{x \rightarrow 0} \frac{1-\cos ^{2}(3 x)}{16 x^{2}}$
b) $\lim _{x \rightarrow 4} \frac{\ln \left(\tan ^{2}\left(\frac{4 \pi}{3 x}\right)\right)-\ln (3)}{2 x^{2}-3 x-20}$

