Name:

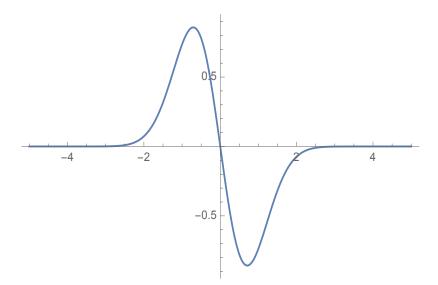
Math 115 Exam 2 $\,$

February 14, 2019

1. WRITE YOUR NAME ON THIS TEST!

- 2. Except where indicated, merely finding the answer to a problem is not enough to receive full credit; you must show how you arrived at that answer.
- 3. Unless indicated, DO NOT convert irrational numbers such as $\sqrt{3}$ or π into decimal approximations; just leave them as they are.
- 4. If you have a question, raise your hand or come up and ask me.

1) (8 points) Below is the graph of a function f. Sketch the graph of f'.



2) Let $f(x) = -7x^5 + 6x^4 - 2x^3 + 5x + 13$.

a) (6 points) Using the definition of the derivative, express the slope of the tangent line to the graph of f at x = 1 as a limit BUT DO NOT COMPUTE THE LIMIT.

b) (9 points) Obtain the equation of the tangent line at x = 1 to the graph of f, using any method at your disposal other than merely your calculator.

- **3)** Calculate f' for the following functions.
 - a) (7 points) $g(x) = \frac{7 3x}{8x + 9}$.
 - b) (10 points) $f(x) = (2x+5)\sqrt{x^4+1}$.

4) Compute the following limits.

a) (10 points)
$$\lim_{\theta \to 0^+} \frac{\sin^2(9\sqrt{\theta})}{2\theta}$$

b) (10 points)
$$\lim_{x \to 2} \frac{\sqrt[3]{5x^2 + 7} - 3}{x - 2}$$

BONUS: (10 points) For ALL odd differentiable functions f, show that f' is even.